

CURVE INTERPOLATION METHOD

BACKGROUND OF THE INVENTION

1. Field of the Invention

The present invention relates to a curve interpolation method for obtaining a smooth curve based on data of a sequence of command points and performing interpolation on the smooth curve in machining a workpiece along a curved surface using a numerical controller.

2. Description of Related Art

In machining a workpiece along a curved surface of an object such as a mold by a numerical controlled machine tool, etc. according to data of a sequence of command points which are created by a CAD/CAM device or a profiler device, a curve interpolation is performed based on the data of the sequence of command points. For example, there is disclosed a method of creating an approximate spline curve based on the data of the sequence of command points and performing the curve interpolation on the created approximate spline curve in JP 2-113305A.

In JP 10-240328A, there is described an interpolation method in which vectors of line segments between adjacent twos of command points are obtained and a modification amount for each command point is obtained such that the sum of squares of differential vectors between the obtained vectors of the line segments is the least so as to modify each command point. In this document, it is described to set an evaluation range in a sequence of the command points and create an approximate curve for successive points in the evaluation range, so that the command points are modified based on differences between the approximate curve and the respective command points in the evaluation range.

In the CAD/CAM device, a tolerance is set for a target curve created by the CAD device and a plurality of line segments are created by the CAM device within the tolerance to obtain data of end points of the respective line

$$f(t)_x = A_x t^3 + B_x t^2 + C_x t + D_x$$

$$f(t)_y = A_y t^3 + B_y t^2 + C_y t + D_y$$

$$f(t)_z = A_z t^3 + B_z t^2 + C_z t + D_z$$

Thus obtained curve Ce is shown in FIG. 20.

Then, interpolation is performed on the defined curve Ce with a unit not greater than a set unit in preparing the sequence of command points (Step S16).

In the foregoing embodiment, at the start of the procedure, all of the command points P0, P1, P2, ... , Pn-1, Pn are read at Step S1. Alternatively, only the necessary command points may be read and the procedure may be carried out on the read points, so that the approximate curve is successively created while reading the data of the command points to expedite the procedure.

In obtaining interpolation points, i.e. shape-defining points, respective two points are interpolated between adjacent twos of the command points in the foregoing embodiment, respective points more than two may be interpolated between adjacent twos of the command points. Further, in creating the approximate curve Cm, the shape-defining points not greater than two are selected before and after the shape-defining point Qi. The shape-defining points greater than two may be selected. Furthermore, one or more of the command points P0, P1, P2, ... , Pn-1, Pn may be used as the shape-defining points with the interpolation points Q1, Q2, ... , Q2n.

If a line segment connecting adjacent two of the command points P0, P1, P2, ... , Pn-1, Pn is shorter than a reference value, an interpolated point Pj' such as a middle point between such adjacent command points Pj, Pj+1 may be regarded as a substitute command point for the adjacent command points Pj, Pj+1 which are to be deleted. In this case, it is determined whether or not a distance between the adjacent command points Pi and Pi+1 is not greater than the predetermined at Step S2, and if the distance is not greater than the predetermined value, the above procedure is performed to define a substitute command point for obtaining the interpolation points.

segments as a sequence of command points to be outputted to the numerical controller.

As shown in FIG. 1, line segments L_0, L_1, L_2, \dots are created by the CAM device within a tolerance width " $2w$ " set by a tolerance amount " w " on both sides of an original target curve C_s which are created by the CAD device, and data of points P_0, P_1, P_2, \dots at both ends of respective line segment L_0, L_1, L_2, \dots are outputted to a numerical controller as data of a sequence of command points. Since a curve C_e for the curve interpolation is defined based on the position data of the sequence of command points, the curve C_e may exceed the tolerance width $2w$ set to the original curve C_s .

According to the method disclosed in JP 10-240328A, the positions of the command points are modified but there is a possibility of creating the curve C_e same as that in FIG. 1 based on the modified command points, and it is not assured that the curve C_e is created within the tolerance width $2w$ set for the original curve C_s .

It is probable that the sequence of command points are positioned near ends of a band of the tolerance width $2w$ set to the original curve C_s . Therefore, if the curve C_e is defined based solely on the sequence of command points, the curve C_e may be positioned considerably remote from the original curve C_s . For instance, in the case where the original curve C_s is a circular arc, as shown in FIG. 2, the command points P_0, P_1, P_2, \dots defined by the line segments L_0, L_1, L_2, \dots within the tolerance width $2w$ are positioned remote from the original curve C_s by an amount approximately equal to the tolerance amount w . In this case, two points Q_1 and Q_2 interpolated on each of the line segments L_0, L_1, L_2, \dots at a ratio of approximately $0.15:0.7:0.15$ are positioned on the original curve C_s , as shown in FIG. 3.

The above circumstance is the same in the case where the positions of the command points are modified. For example, in the case where the original curve is a circular arc, since a sequence of command points are aligned along a circular arc, if a curve approximating the command points is created, the sequence of command points are not substantially modified. Thus, the modified sequence of command points are positioned remote from the original curve C_s by the tolerance amount w .

Since the curve C_e is defined to pass the sequence of command points P_0, P_1, P_2, \dots , if there is an error in calculation for obtaining the sequence of command points P_0, P_1, P_2, \dots or in approximation by a set unit in the CAD/CAM device, the error influences the definition of the curve C_e to lower machining precision and cause a vibration of the machine. Thus, the definition of the curve C_e to pass the sequence of command points may cause deterioration of the precision of the machined surface.

SUMMARY OF THE INVENTION

An object of the present invention is to provide a curve interpolation method capable of obtaining a curve approximating an original target curve within a tolerance set for the original target curve based on a sequence of command points, and performing interpolation on the obtained curve.

As describe, the command points P_0, P_1, P_2, \dots are positioned within the tolerance width $2w$ and the line segments L_0, L_1, L_2, \dots connecting the adjacent twos of the command points $(P_0, P_1), (P_1, P_2), \dots$ are positioned within the tolerance width $2w$, as shown in FIG. 5. Therefore, points Q_1, Q_2, Q_3, \dots interpolated on the respective line segments L_0, L_1, L_2, \dots are positioned within the tolerance width $2w$. According to the present invention, a smooth curve C_e approximating an original curve C_s is defined using the interpolated points Q_1, Q_2, Q_3, \dots , and a curve interpolation for machining a workpiece is performed on the smooth curve C_e by a procedure comprising the following steps (1)-(7).

(1) Interpolation points Q_1, Q_2, Q_3, \dots are defined between adjacent twos of the command points $(P_0, P_1), (P_1, P_2), \dots$, as shape-defining points. The shape-defining points Q_1, Q_2, Q_3, \dots are positioned inner the band of the tolerance width $2w$, i.e. closer to the original curve C_s than the command points P_0, P_1, P_2, \dots .

(2) One shape-defining point Q_i and adjacent shape-defining points in front of and in the rear of the one shape-defining point Q_i to be surrounded by these adjacent points are selected.

(3) A curve C_m approximating the selected shape-defining points is created, as shown in FIG. 6.

(4) The one shape-defining point Q_i is moved towards the approximate curve C_m to define the modified command point Q_i' .

(5) Repeatedly executing the above steps (2)-(4) successively on the other shape-defining points to obtain the modified shape-defining points Q_1' , Q_2' , Q_3' ,

(6) A curve C_e passing the modified command points Q_0' , Q_1' , Q_2' , ... is defined.

(7) The interpolation is performed on the obtained curve C_e .

In the step (1), one or more of the command points P_0 , P_1 , P_2 , ... may be used as the shape-defining points in addition to the interpolated points Q_1 , Q_2 , Q_3 , In this step (1), the interpolation points Q_1 , Q_2 , Q_3 , ... are created with a unit not greater than a set unit in preparing the sequence of command points P_0 , P_1 , P_2 , ...

In the step (1), if a distance between adjacent two of the command points P_j , P_{j+1} is shorter than a first reference value, an interpolation point P_j' between the adjacent two command points P_j , P_{j+1} is used as a substitute therefor, as shown in FIG. 7. The interpolated point may be a middle point of the adjacent two command points P_j , P_{j+1} .

In the step (3), the approximate curve C_m may be created to have the least sum of squares of distances from the selected shape-defining points.

In the step (4), an amount of moving the one shape-defining point Q_i for modification may be restricted to a set value.

In the step (4), if a distance between adjacent two of the modified shape-defining points Q_j' , Q_{j+1}' is shorter than a second reference value, an interpolation point Q_j'' between the adjacent two modified shape-defining points Q_j' , Q_{j+1}' is used as a substitute for the two modified shape-defining points, as shown in FIG. 8. The interpolated point Q_j'' may be a middle point of the adjacent two modified shape-defining points Q_j' , Q_{j+1}' .

In the step (4), the one shape defining point Q_i may be moved gradually

with a unit not greater than a set unit in preparing the sequence of command points P_0, P_1, P_2, \dots

In the step (6), first-order differentiate values $Q_0^{(1)}, Q_1^{(1)}, Q_2^{(1)}, \dots$ of the approximate curve C_m at points corresponding to the modified shape-defining points Q_0', Q_1', Q_2', \dots are used in creating the curve C_e passing a sequence of modified shape-defining points Q_0', Q_1', Q_2', \dots , as shown in FIG. 9.

In the step (6), the curve C_e passing the modified command points Q_0', Q_1', Q_2', \dots may be a NURBS curve or a spline curve.

In the step (7), the interpolation on the obtained curve C_e is performed with a unit not greater than a set unit in preparing the sequence of command points P_0, P_1, P_2, \dots

BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 is a schematic diagram showing a conventional interpolation method in which a curve is created based on a sequence of command points;

FIG. 2 is a schematic diagram showing an original target curve and a created curve in a case where the original target curve is a circular arc;

FIG. 3 is a schematic diagram showing intersection between the original target curve and line segments connecting adjacent two of the command points in the conventional interpolation method;

FIG. 4 is a schematic diagram showing an example of an inappropriate curve created from the command points according to the conventional method;

FIG. 5 is a schematic diagram showing interpolation points used as shape-defining points according to the present invention;

FIG. 6 is a schematic diagram showing movement of the shape-defining point toward the approximate curve to obtain a modified shape-defining point;

FIG. 7 is a schematic diagram showing substitution of command points;

FIG. 8 is a schematic diagram showing substitution of modified shape-defining points;

FIG. 9 is a schematic diagram showing a first-order differentiated value for a modified shape-defining point;

FIG. 10 is a block diagram of a numerical controller for carrying out the method of the present invention;

FIG. 11 is a schematic diagram showing a part of a machining program for executing the curve interpolation according to the present invention;

FIG. 12 is a schematic diagram of a sequence of command points for which automatic determination of carrying out the curve interpolation of the present invention is performed;

FIG. 13 is a schematic diagram of a sequence of command points for which another automatic determination of carrying out the curve interpolation of the present invention is performed;

FIG. 14 is a part of flowchart of processing for the curve interpolation according to the present invention;

FIG. 15 is a continuation of the flowchart of FIG. 14;

FIG. 16 is a schematic diagram of a sequence of command points;

FIG. 17 is a schematic diagram showing interpolation points between adjacent twos of the command points for obtaining shape-defining points;

FIG. 18 is a schematic diagram showing an approximate curve for the shape-defining points for obtaining a modified shape-defining point and a first-order differentiated value therefor;

FIG. 19 is a schematic diagram showing a substitute point to be substituted for adjacent two modified shape-defining points and a substitute first-order differentiated value therefor; and

FIG. 20 is a schematic diagram showing an example of a smooth curve created according to the present invention.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

FIG. 10 shows a numerical controller 100 for carrying out the curve interpolating method of the present invention.

A processor (CPU) 11 for generally controlling the numerical controller 100 is connected with a memory 12 including a ROM, a RAM and a CMOS memory backed up by a battery; an interface 13 to which a data input/output device 34 is connected; an interface 16 to which a display/MDI unit 30 is connected; an interface 17 to which an operation panel 31 is connected; a PC (programmable controller) 14; a display/MDI unit 30; axis control circuits 18; and a spindle control circuit 20, through a bus 22.

The axis control circuits 18 output commands to the servo amplifiers 19 for respective axes in accordance with motion commands from the processor 11. The servo amplifiers 19 drive servomotor 32 for the respective axes in accordance with the commands from the axis control circuits 18. Each of the servomotors 32 has a position/velocity detector (not shown) for feeding back position/velocity feedback signals to the associated axis controller 18 for feedback control of the position/velocity of the axis.

The spindle control circuit 20 outputs a spindle speed signal to the spindle amplifier 21 based on a spindle speed command from the processor 11 and a speed feedback signal from a position coder provided at the spindle motor 33. The spindle amplifier 21 drives the spindle at the commanded speed in accordance with the spindle speed command.

A machining program including data of the command points created by the CAD/CAM device or a profile device is inputted into the numerical controller 100 from the data input/output device 34 through the interface 13 and stored in the nonvolatile section of the memory 12.

G-codes commanding a start of defining a smooth curve and interpolation thereon, and commanding discontinuation of the command are prepared. A G-code "G06.3" for commanding a start of defining a smooth curve and interpolation thereon is programmed at the beginning of data of a sequence of command points, and a G-code "G06.9" is programmed at a position where this command is to be discontinued in the machining program.

The procedure of defining a smooth curve and interpolation thereon is carried out in a section between the codes "G06.3" and "G06.9".

The section in which definition of a smooth curve and interpolation thereon are performed may be automatically determined. In this case, the processor 11 reads the sequence of command points from the machining program and determines whether or not the creation and interpolation of the smooth curve is to be performed based on angles between adjacent ones of the line segments or lengths of the line segments interconnecting the adjacent ones of the command points. As shown in FIG. 12, angles between adjacent line segments interconnecting adjacent ones of command points P1, P2, P3 and command points P6, P7, P8 are smaller than a reference value. Thus, it is determined that a smooth curve is to be created and interpolated in these sections. Contrary, an angle α between a line segment interconnecting command points P3 and P4 and a line segment interconnecting command points P4 and P5 are relatively large. Similarly, an angle β between the line segment interconnecting command points P4 and P5 and a line segment interconnecting command points P5 and P6 is larger than the reference value. Thus, it is determined that a smooth curve is not to be created and interpolated in the section between the command points P4 and P5. Namely, if an angle between the line segments interconnecting the adjacent command points is not greater than the reference value, it is automatically determined that a smooth curve is to be created and interpolated in the section of the line segment, and if the angle between the line segments interconnecting the adjacent command points is less than the reference value, it is automatically determined that a smooth curve is not to be created and interpolated.

Further, as shown in FIG. 13, distances between the adjacent command points from the command point P1 to the command point P4, and from the command point P5 to the command point P8 are relatively short, and a distance between the command point P4 and the command point P5 is relatively long. Thus, if the distance between the adjacent command points is not greater than a reference value, it is determined that a smooth curve is to be created and interpolated in the section defined by such command points, and if the distance between the adjacent command points is greater than a reference value, it is

determined that a smooth curve is not to be created and interpolated in the sections between such command points.

The processing for defining a smooth curve and interpolation thereon will be described referring to flowcharts of FIGS. 14 and 15.

The processor 11 reads a sequence of command points $P_0, P_1, \dots, P_{n-1}, P_n$ from a machining program (Step S1). An example of the read command points $P_0, P_1, \dots, P_{n-1}, P_n$ are shown in FIG. 16.

Respective two interpolation points $(Q_1, Q_2), (Q_3, Q_4), \dots, (Q_{2n-1}, Q_{2n})$ are defined between the adjacent two command points $(P_0, P_1), (P_1, P_2), \dots, (P_{n-1}, P_n)$ (Step S2). In this example, an interpolation ratio is set to $1:0.7:0.15$, as shown in FIG. 17. In particular, the interpolation ratio of interpolation points (Q_{2i+1}, Q_{2i+2}) on a line segment (P_i, P_{i+1}) is set such that a length of a line segment (P_i, P_{i+1}) : a length of a line segment (Q_{2i+1}, Q_{2i+2}) : a length of a line segment $(P_i, Q_{2i+1}) = 1:0.7:0.15$.

A first shape-defining point Q_0 is set to P_0 and a last shape-defining point Q_{2n+1} is set to P_n (Step S3). Thus, a sequence of shape-defining points comprising a sequence of interpolation points $Q_0, Q_1, Q_2, \dots, Q_{2n}, Q_{2n+1}$ are created.

Then, the index i is initially set to "1" in Step S4. A value of the index i is determined in Steps S5 and S6, and if it is determined that the index i is "1", the shape-defining points $Q_{i-1}, Q_i, Q_{i+1}, Q_{i+2}$ ($=Q_0, Q_1, Q_2, Q_3$) are selected (Step S17), if it is determined that the index i is "2, 3, ..., or $2n-1$ ", the shape-defining points $Q_{i-2}, Q_{i-1}, Q_i, Q_{i+1}, Q_{i+2}$ are selected (Step S7), and if the index i is determined as " $2n$ ", the shape-defining points $Q_{i-2}, Q_{i-1}, Q_i, Q_{i+1}$ ($=Q_{2n-2}, Q_{2n-1}, Q_{2n}, Q_{2n+1}$) are selected (Step S18). If the index i is determined as " $2n+1$ ", the procedure as described later is performed.

An approximate curve C_m is created based on thus selected shape-defining points by the least-squares method. Namely, the curve C_m having the least sum of squares of distances from the selected shape-defining points is defined (Step S8). An example of the approximate curve C_m is shown as the one-dotted chain line in FIG. 18. The shape-defining point Q_i designated by the present value of the index i is moved towards the

approximate curve C_m gradually with a unit not greater than a set unit in preparing the sequence of command points and within the tolerance width $2w$ to define a modified shape-defining point Q_i' with respect to the shape-defining point Q_i (Step S9). A first-order differentiated value $Q_i^{(1)'}$ of the modified shape-defining point Q_i' on the approximate curve C_m is obtained and stored (Step S10).

The index i is incrementally increased by "1" (Step S11), and it is determined whether or not the value of the index i exceeds " $2n+1$ " which is the index of the last shape-defining point Q_{2n+1} (Step S12). If it is determined that the index i does not exceed " $2n+1$ ", the procedure returns to Step S5 to repeat the processing of Step S5 and subsequent Steps.

When it is determined that the index i reaches " $2n+1$ " in Step S5, a modified shape-defining point Q_{2n+1}' is set as the command point P_n , and an orientation vector from the modified shape-defining point Q_{2n}' to the command point P_n is stored as a first-order differentiated value $Q_{2n+1}^{(1)'}$ with respect to the modified shape-defining point Q_{2n+1}' (Step S19). Then, the index i is incrementally increased by "1" (Step S11). As a result, it is determined that the index i exceeds " $2n+1$ " which is the index of the last shape-defining points Q_{2n+1} (Step S12), and the procedure proceeds to Step S13 where the modified shape-defining point Q_0' is set as the command point P_0 , and an orientation vector from the command point P_0 to the modified shape-defining point Q_1' is set to a first-order differentiated value $Q_0^{(1)'}$ with respect to the modified shape-defining point Q_0' ($=P_0$). With the above processing, the modified shape-defining points $Q_0', Q_1', Q_2', \dots, Q_{2n}', Q_{2n+1}'$ and the first-order differentiated values $Q_0^{(1)'}, Q_1^{(1)'}, Q_2^{(1)'}, \dots, Q_{2n}^{(1)'}, Q_{2n+1}^{(1)'}$ with respect to the shape-defining points $Q_0, Q_1, Q_2, \dots, Q_{2n}, Q_{2n+1}$ are calculated.

Further, in this embodiment, as shown in FIG. 19, if there are two adjacent modified shape-defining points Q_j' and Q_{j+1}' having a distance therebetween shorter than a reference value in the modified shape-defining points $Q_0', Q_1', \dots, Q_{2n+1}'$, an interpolation point is created between the two points Q_j' and Q_{j+1}' . In this embodiment, a middle point of the two points Q_j' and Q_{j+1}' is used as a substitute for the modified shape-defining points Q_j' and

Q_{j+1}' which are to be deleted. Also, an average value of the first-order differentiated values $Q_j^{(1)}$ and $Q_{j+1}^{(1)}$ for the modified shape-defining points Q_j' and Q_{j+1}' is set as a substituted first-order differentiated value $Q_j^{(1)}$ for the substituted modified shape-defining point Q_j' , and the original first-order differentiated values $Q_j^{(1)}$ and $Q_{j+1}^{(1)}$ are deleted. The first modified shape-defining point Q_0' and the last modified shape-defining point Q_{2n+1}' of the sequence of modified shape-defining points and the first-order differentiated values $Q_0^{(1)}$ and $Q_{2n+1}^{(1)}$ for the first and last modified shape-defining points Q_0' and Q_{2n+1}' are not deleted.

With the above procedure, the modified shape-defining points Q_0' , Q_1' , ..., Q_{2n+1}' and the first-order differentiated values $Q_0^{(1)}$, $Q_1^{(1)}$, ..., $Q_{2n+1}^{(1)}$ for the modified shape-defining points Q_0' , Q_1' , ..., Q_{2n+1}' are obtained (Step S14).

Then, a curve C_e passing the modified shape-defining points Q_0' , Q_1' , ..., Q_{2n+1}' is obtained based on the position data of the modified shape-defining points Q_0' , Q_1' , ..., Q_{2n+1}' and the first-order differentiated values $Q_0^{(1)}$, $Q_1^{(1)}$, ..., $Q_{2n+1}^{(1)}$ (Step S15).

For instance, since position data of the two shape-defining points Q_j' , Q_{j+1}' and the first-order differentiated values $Q_j^{(1)}$, $Q_{j+1}^{(1)}$ at the respective shape-defining points Q_j' , Q_{j+1}' are given, a third-order curve such as a spline curve or a NURBS curve passing these points can be defined. More specifically, in the case of defining a third-order curve by a spline curve connecting the two points Q_j' and Q_{j+1}' , coefficients A , B , C and D in the following equation representing the spline curve are determined based on the position data of the two points Q_j' and Q_{j+1}' and the first-order differentiated values $Q_j^{(1)}$ and $Q_{j+1}^{(1)}$, and thus the three-order curve C_e is created to connect the two points Q_j' and Q_{j+1}' (Step S15).

$$f(t) = At^3 + Bt^2 + Ct + D$$

where A , B , C and D are coefficients and " t " is a curve parameter ranging from 0 to 1.0

$f(t)$, A , B , C and D are vectors having values with respect to each axis of x , y and z .

In the foregoing embodiment, an interpolation ratio, i.e. the interpolation ratio of the interpolation points (Q_{2i+1} , Q_{2i+2}) between the line segment (P_i , P_{i+1}) is the distance between the line segment (P_i , P_{i+1}): the line segment (Q_{2i+1} , Q_{2i+2}): the line segment (P_i , P_{2i+1}) = 1: 0.7 : 0.15. The interpolation ratio may be other value.

According to the present invention, a smooth curve approximating an original target curve within a tolerance set to the original target curve is obtained based on a sequence of command points and interpolation for machining is performed on the obtained curve.